

# Survival of the Fittest

Daniel Meier, 08 October 2025

# Relevant articles

## Survival of the Fittest: Classical and Machine Learning Methods for Time-to-Event Modeling

Daniel Meier\*      Adam Sturge†

Prepared for:  
Fachgruppe “Data Science”  
Swiss Association of Actuaries SAV  
Version of August 31, 2025

### Abstract

This tutorial provides an overview of classical and machine learning methods for survival modeling. We start with introducing the basic concepts of survival modeling using the Cox proportional hazards model and the accelerated failure time model, highlighting their

Case study 16 on [actuarialdatascience.org](https://actuarialdatascience.org)

GLP-1 weight loss drugs on [swissre.com](https://swissre.com)

# GLP-1 drugs started out as a niche diabetes treatment but have become big business



*Heavy guy, light appetite: this gila monster eats a few times a year, slowly digesting his food thanks to his naturally long-lasting GLP-1 hormone*

## Future trends in drug development



**More targets:** semaglutide: 1 target. Tirzepatide: 2 targets. New drugs: 2-3+ targets and/or combinations



**Different doses:** today the standard is weekly injections. Trials are for fortnightly or monthly injections. Daily tablets are in development



**Fast weight loss:** companies are targeting headline large losses of weight over as little time as possible

## CURRENTLY USED

Previous generation medications

**Ozempic/Wegovy**  
Semaglutide (2021)  
**Format:** once-weekly injectable



**Zepbound/Mounjaro**  
Tirzepatide (2023)  
**Format:** once-weekly injectable



## IN DEVELOPMENT

**Rybelsus**



**Year:** 2025 – approved for diabetes, pending approval for weight loss  
**Format:** daily oral tablet

**Orforglipron**



**Year:** 2025 – phase 3 clinical trial  
**Format:** daily oral tablet

**Others**  
- multitude of developers trialing different receptors, dosages, regimes and delivery mechanisms

**MariTide**



**Year:** 2024 – phase 2 clinical trial  
**Format:** monthly injectable

**AZD5004**



**Year:** 2024 – phase 1 clinical trial  
**Format:** daily oral tablet

**CT-996**



**Year:** 2025 – phase 1 clinical trial  
**Format:** daily oral tablet

**How they work:** slow gastric emptying, creating a feeling of satiety, reduce calories

# Promising short-term clinical trial results: long-term real-world effectiveness is pending

	<b>Semaglutide</b> (Ozempic/ Wegovy)	<b>Tirzepatide</b> (Mounjaro/ Zepbound)
In the head-to-head study over 72 weeks:		
Weight lost (kg)	↓ 15.0	22.8
Weight loss (%)	↓ 13.7	20.2
Waist circumference (cm)	↓ 13.0	18.4
BMI points	↓ 5.3	8.0

Additional improvements in blood pressure, HbA1c and cholesterol markers were seen in both drugs but superior for tirzepatide



Tirzepatide beat semaglutide in every category



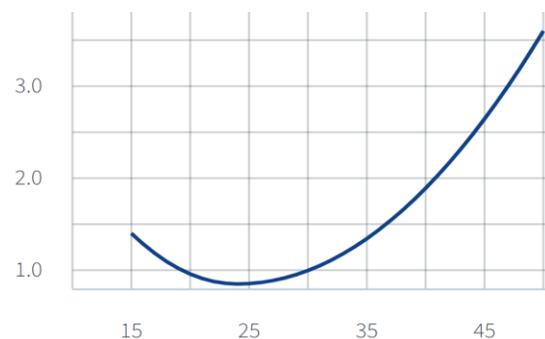
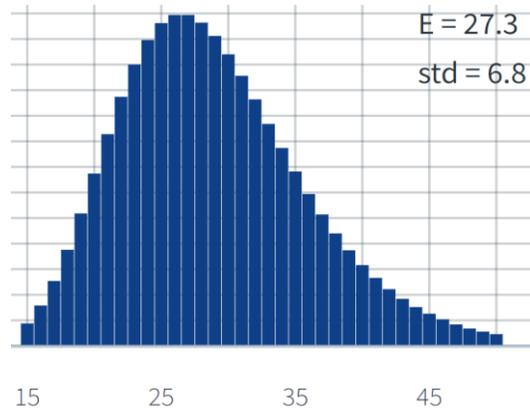
Between 39% (semaglutide) and 18% (tirzepatide) participants didn't lose  $\geq 10\%$  weight

Caveat: clinical trial results do not directly translate into real-world results. Longer-term considerations include drug adherence and sustained weight loss.

# Metabolic health model combines expert elicitation with comprehensive data

## Data inputs

BMI **distribution** and **relative mortality** risk by age, SES, country



## Analysis process



Expert elicitation on BMI & GLP-1



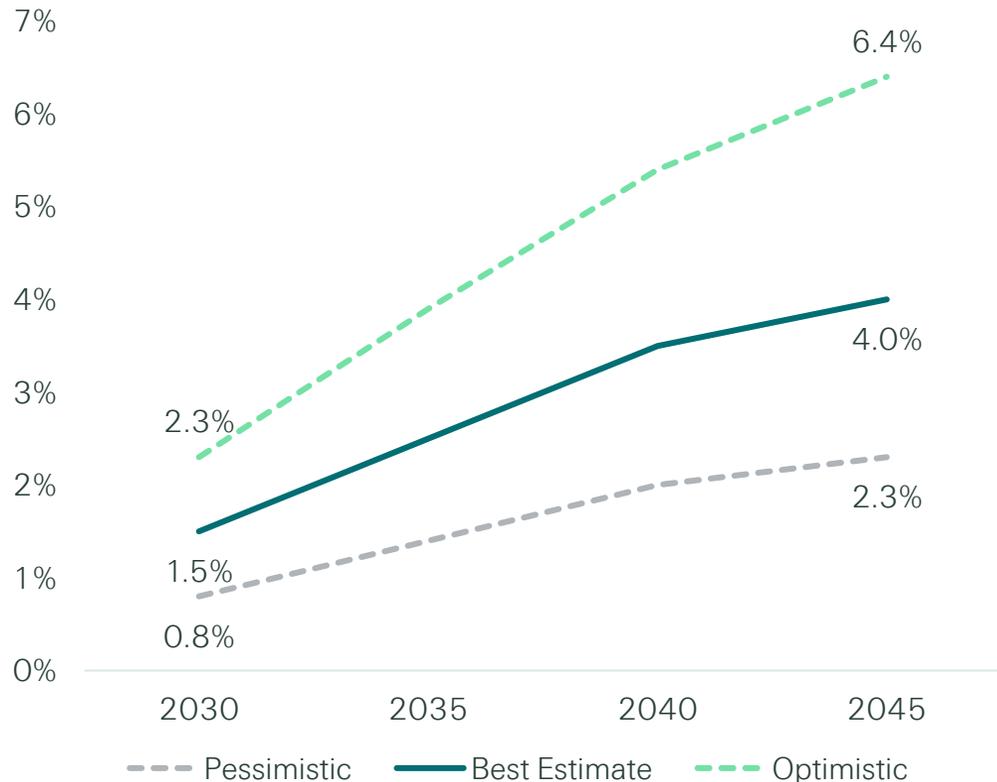
Literature review on all factors

## Modelling output

- **Population:** general and insured population
- **Countries:** US, China, UK
- **Timeframe:** 2025 – 2045
- **Scenarios:**
  1. Best estimate
  2. Optimistic
  3. Pessimistic
- **Methodology:** simulates 100k individuals with a given age, SES, BMI, SBP, etc.
- **Output:** aggregates total relative mortality risk distributions

# US general population: best estimate mortality reduction of 4.0% by 2045

## US general population projection



## Rationale



**Broad starting health:** US general population has a wide range of health statuses



**Lifestyle changes:** behavioural adaptations support medium- and long-term mortality benefits



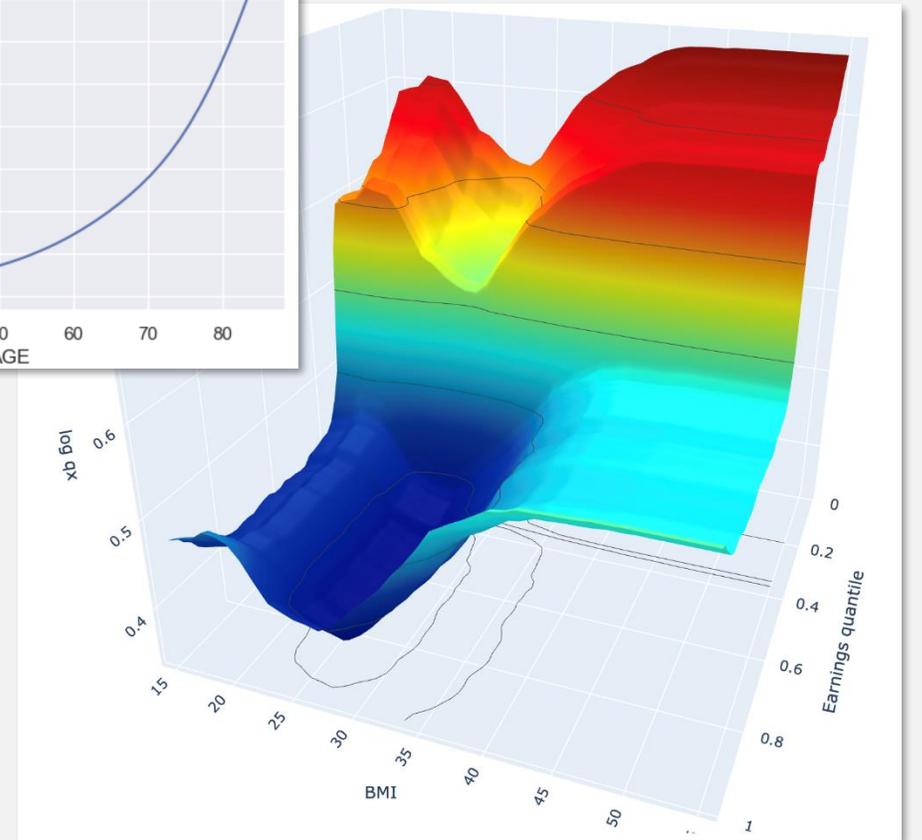
**Age:** middle-aged population is expected to see the largest mortality benefits



**Greatest opportunity:** widespread metabolic health changes would see substantial public health improvements

# Where is survival modelling applied?

- Life & Health Underwriting
- Scenario testing, e.g., weight loss drugs
- US cancer registry SEER: Underwriting
- CIA pensioner mortality tables
- Unemployment times
- Public health
- Any other use case where **time-to-event** is important, e.g., credit default, lapse, engineering, etc.



# Linear regression

$$y(x) = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_M x_M$$

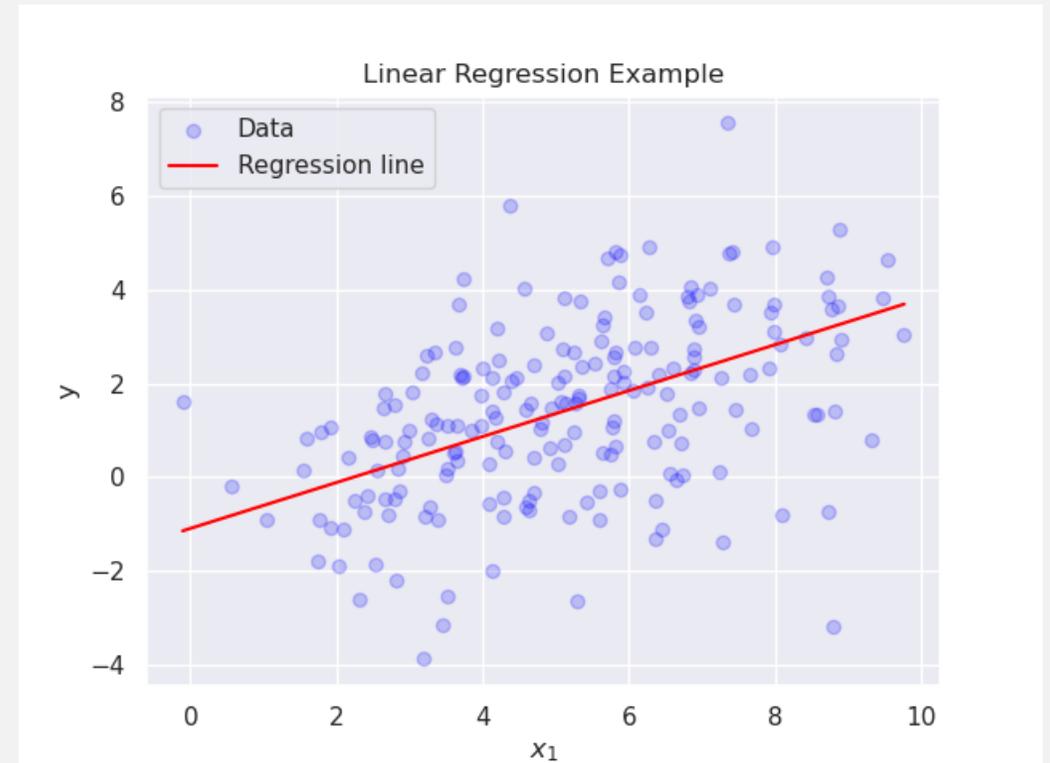
OLS Regression Results

```
=====
Dep. Variable:          y      R-squared:          0.738
Model:                 OLS    Adj. R-squared:     0.734
Method:                Least Squares  F-statistic:       184.4
Date:                  Fri, 15 Aug 2025  Prob (F-statistic): 8.17e-57
Time:                  14:50:57  Log-Likelihood:    -277.39
No. Observations:     200      AIC:               562.8
Df Residuals:         196      BIC:               576.0
Df Model:              3
Covariance Type:      nonrobust
=====
```

	coef	std err	t	P> t	[0.025	0.975]
const	2.1888	0.293	7.458	0.000	1.610	2.768
x1	0.4899	0.034	14.387	0.000	0.423	0.557
x2	-0.3280	0.025	-13.149	0.000	-0.377	-0.279
x3	1.1735	0.068	17.172	0.000	1.039	1.308

```
=====
Omnibus:                0.265  Durbin-Watson:        2.082
Prob(Omnibus):          0.876  Jarque-Bera (JB):     0.402
Skew:                   0.064  Prob(JB):              0.818
Kurtosis:               2.822  Cond. No.              48.1
=====
```

statsmodels summary



# Logistic regression

$$p(x) = \text{logistic}(\beta_0 + \beta_1 x_1 + \beta_2 x_2 + \dots + \beta_M x_M)$$
$$\text{logistic}(x) = (1 + \exp(-x))^{-1}$$

## Logit Regression Results

```
=====
Dep. Variable:          y      No. Observations:      200
Model:                 Logit  Df Residuals:         196
Method:                MLE    Df Model:              3
Date:                  Fri, 15 Aug 2025  Pseudo R-squ.:      0.4304
Time:                  14:48:34  Log-Likelihood:       -66.445
converged:              True    LL-Null:              -116.65
Covariance Type:      nonrobust  LLR p-value:         1.266e-21
=====
```

	coef	std err	z	P> z	[0.025	0.975]
const	0.9304	0.915	1.017	0.309	-0.863	2.723
x1	0.8313	0.155	5.354	0.000	0.527	1.136
x2	-0.6647	0.112	-5.961	0.000	-0.883	-0.446
x3	1.1915	0.270	4.413	0.000	0.662	1.721

statsmodels summary

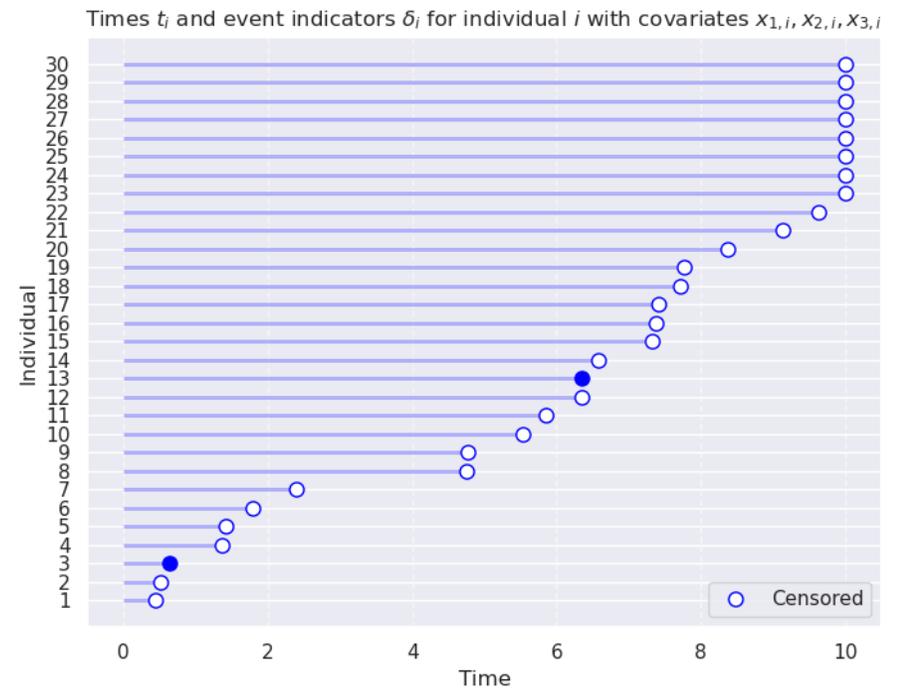


# Cox regression

(the most common survival model)

$$h(t|\mathbf{x}) = h_0(t) \exp(\beta_1 x_1 + \beta_2 x_2 + \dots + \beta_M x_M)$$

- **Data** consists of individuals  $i$  with
  - features  $x_{1,i}, x_{2,i}, \dots$
  - time  $t_i$
  - event indicator  $\delta_i$ , where
    - $\delta_i = 0$  denotes (right-)censoring
    - $\delta_i = 1$  denotes, e.g., mortality
- What is the distribution (CDF  $F$ , PDF  $f$ ) of survival time  $T$ ?

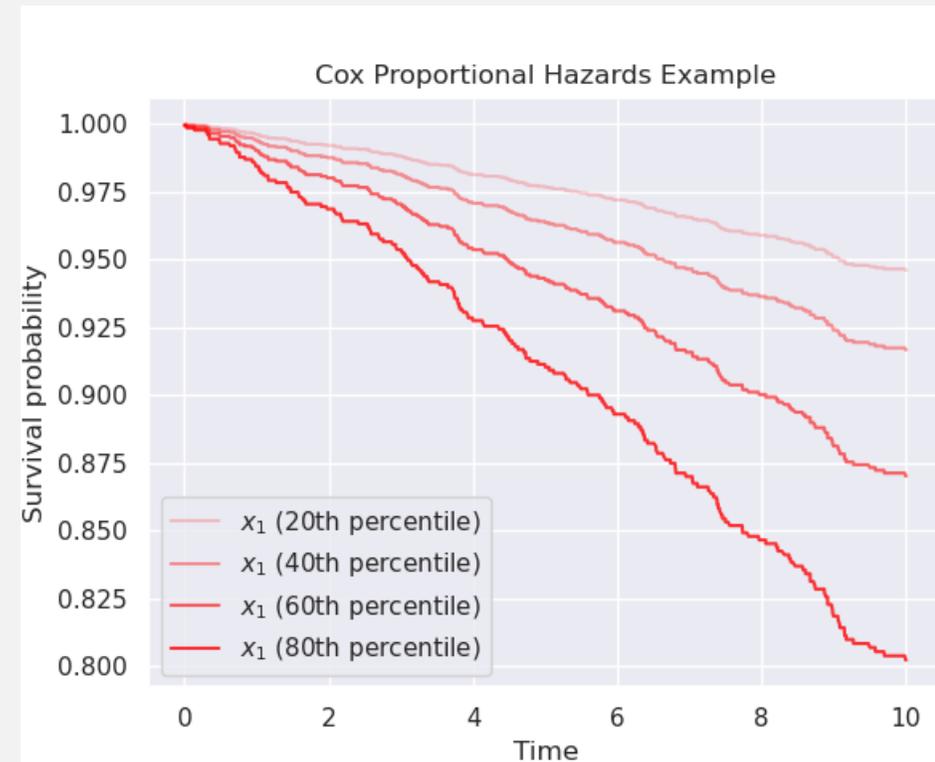


# Cox regression

(the most common survival model)

$$h(t|\mathbf{x}) = h_0(t) \exp(\beta_1 x_1 + \beta_2 x_2 + \dots + \beta_M x_M)$$

- **Hazard rates**  $h(t|\mathbf{x})$ , correspond to force of mortality  $\mu_x(t)$  in continuous time and  $q_{x,t}$  or  $m_{x,t}$  in discrete time
- **Proportional hazards:**  $h(t|\mathbf{x}_i)/h(t|\mathbf{x}_j)$  const.
- **Survival probability function**  $S(t|\mathbf{x})$ , corresponds to  ${}_t p_x$
- $S(t|\mathbf{x}) = 1 - F(t|\mathbf{x})$
- $h(t|\mathbf{x}) = -\frac{\partial}{\partial t} \log S(t|\mathbf{x}) = \frac{f(t|\mathbf{x})}{S(t|\mathbf{x})}$



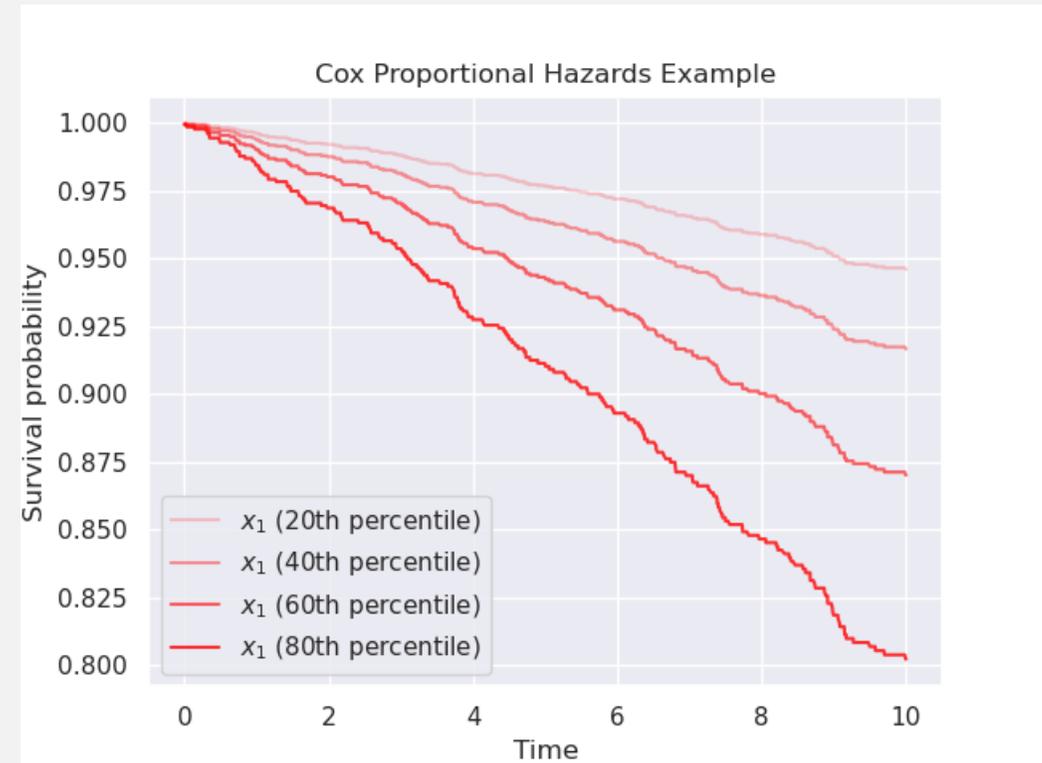
# Cox regression

(the most common survival model)

$$h(t|\mathbf{x}) = h_0(t) \exp(\beta_1 x_1 + \beta_2 x_2 + \dots + \beta_M x_M)$$

- **Baseline hazard rates**  $h_0(t)$  via
  - Kaplan-Meier:  $S(t) = \prod_{t_i \leq t} \left(1 - \frac{d_i}{n_i}\right)$
  - Nelson-Aalen:  $H(t) = \sum_{t_i \leq t} \frac{d_i}{n_i}$
- **Coefficients**  $\beta_1, \beta_2, \dots$  via partial likelihood function maximization (Breslow method)

$$\mathcal{L} = \prod_{i:\delta_i=1} \prod_{j:t_j=t_i} \frac{\exp(\beta_1 x_{1,j} + \dots)}{\sum_{k:t_k \geq t_j} \exp(\beta_1 x_{1,k} + \dots)}$$



## A bit of public health history...

Lester Breslow (1915-2012), the father of Norman Breslow after whom the method was named

**D**r. **Lester Breslow**, a former dean of the UCLA Jonathan and Karin Fielding School of Public Health, professor emeritus of health services, and one of the leading figures in public health for seven decades, died Monday. He was 97.

Breslow was a visionary public health figure with a well-established track record for being ahead of his time. As early as the 1940s, he linked tobacco use to disease in three studies that were later cited in the U.S. Surgeon General's landmark 1964 report.

He is widely known for his early advocacy and research into health promotion and disease prevention. Breslow's pioneering Alameda County studies beginning in the early 1960s were among the first to show that simple health practices — such as getting regular exercise and sleep, not drinking excessively, not smoking, and maintaining a healthy weight — add both years and quality to life.

While these conclusions are taken for granted today, the idea of such a strong connection between lifestyle and health was seen as "bizarre" at the time, Breslow noted decades later. He would smile when recalling the response of the National Institutes of Health panel of scientists that reviewed the initial study proposal: "Unanimous rejection." When the study was completed, even Breslow was shocked at the magnitude of the results, which helped usher in current thinking about health and fitness.

Source: <https://ph.ucla.edu/news-events/news/memorial-dr-lester-breslow-public-health-visionary>

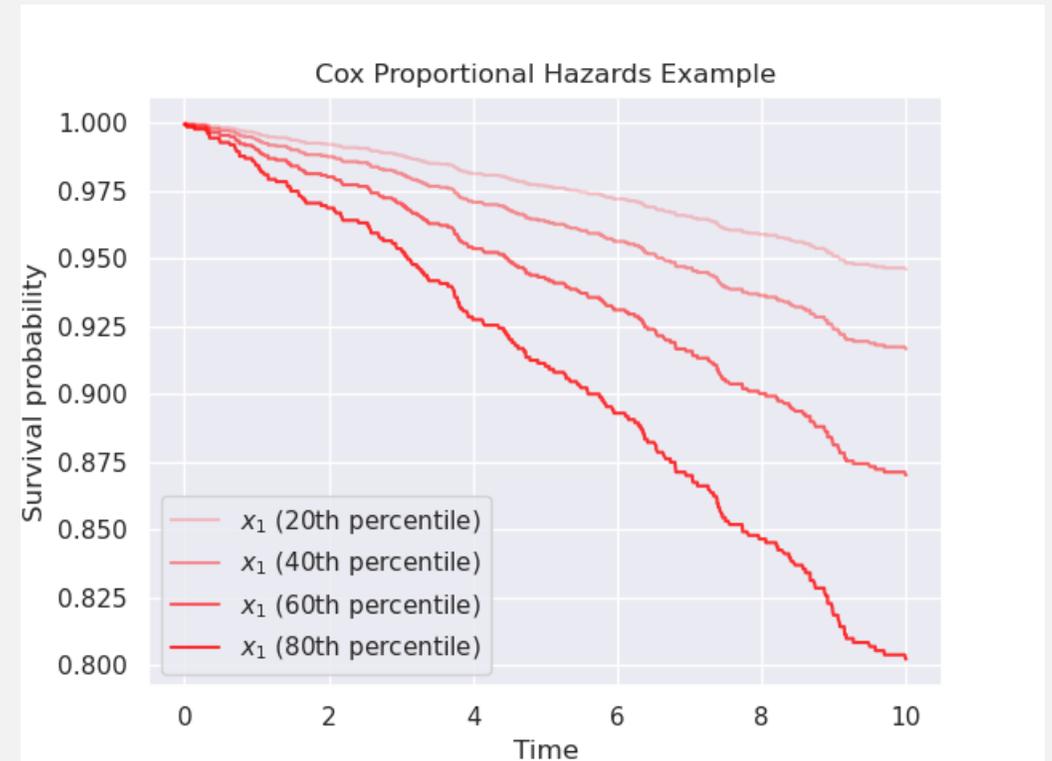
# Cox regression

(the most common survival model)

$$h(t|\mathbf{x}) = h_0(t) \exp(\beta_1 x_1 + \beta_2 x_2 + \dots + \beta_M x_M)$$

<b>model</b>	lifelines.CoxPHFitter										
<b>duration col</b>	'time'										
<b>event col</b>	'event'										
<b>baseline estimation</b>	breslow										
<b>number of observations</b>	2000										
<b>number of events observed</b>	178										
<b>partial log-likelihood</b>	-1248.33										
<b>time fit was run</b>	2025-08-18 08:31:08 UTC										
	<b>coef</b>	<b>exp(coef)</b>	<b>se(coef)</b>	<b>coef lower 95%</b>	<b>coef upper 95%</b>	<b>exp(coef) lower 95%</b>	<b>exp(coef) upper 95%</b>	<b>cmp to</b>	<b>z</b>	<b>p</b>	<b>-log2(p)</b>
<b>x1</b>	0.09	1.09	0.01	0.07	0.11	1.07	1.12	0.00	7.76	<0.005	46.71
<b>x2</b>	0.20	1.22	0.15	-0.09	0.50	0.91	1.64	0.00	1.34	0.18	2.46
<b>x3</b>	0.04	1.04	0.02	0.00	0.07	1.00	1.08	0.00	2.06	0.04	4.67
<b>Concordance</b>	0.67										
<b>Partial AIC</b>	2502.65										
<b>log-likelihood ratio test</b>	72.86 on 3 df										
<b>-log2(p) of ll-ratio test</b>	49.77										

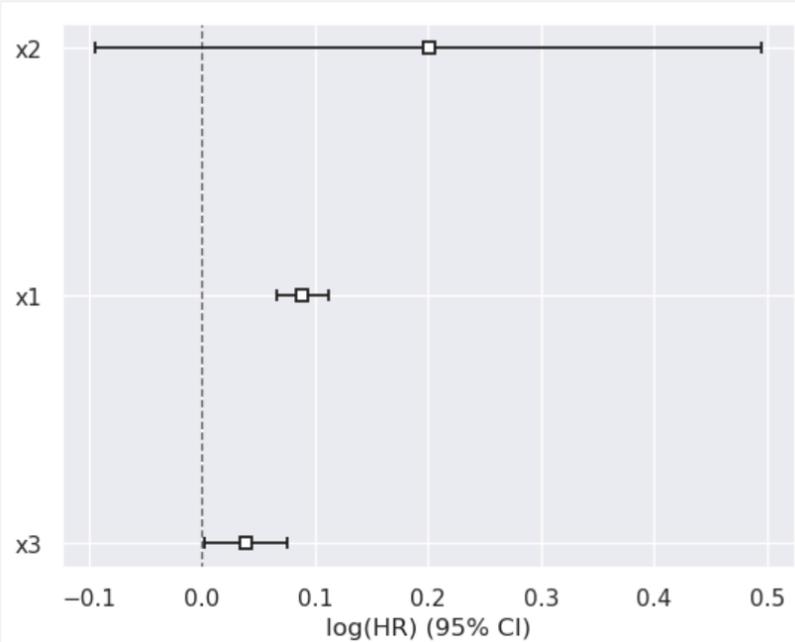
lifelines summary



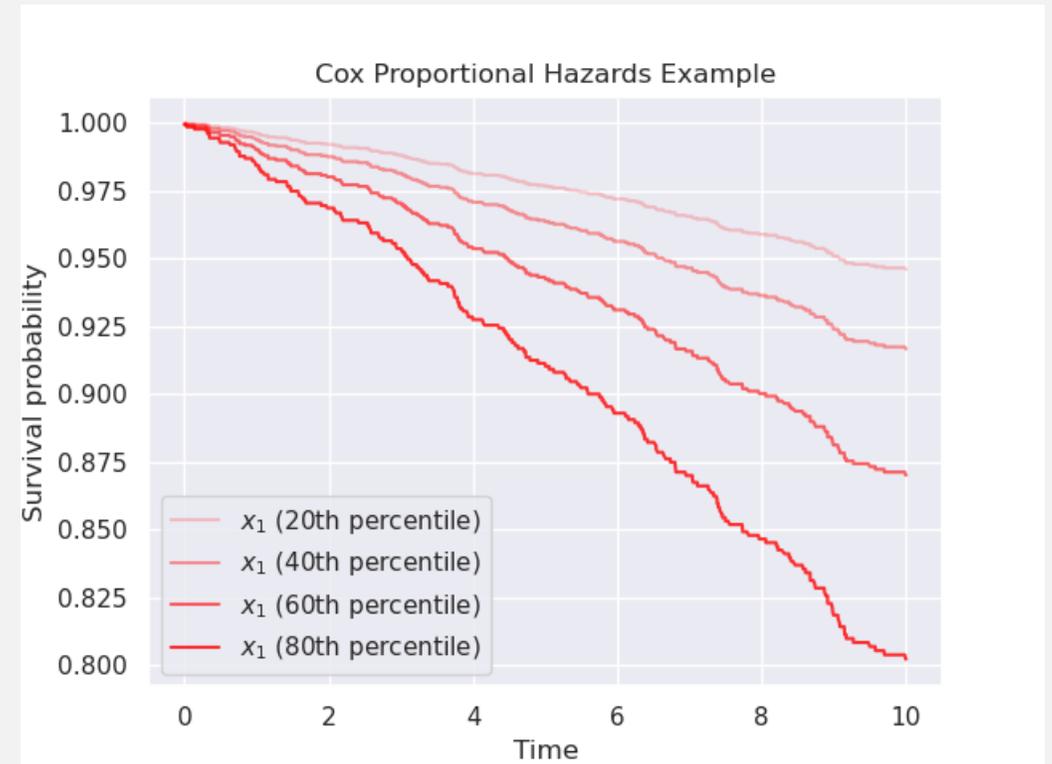
# Cox regression

(the most common survival model)

$$h(t|\mathbf{x}) = h_0(t) \exp(\beta_1 x_1 + \beta_2 x_2 + \dots + \beta_M x_M)$$

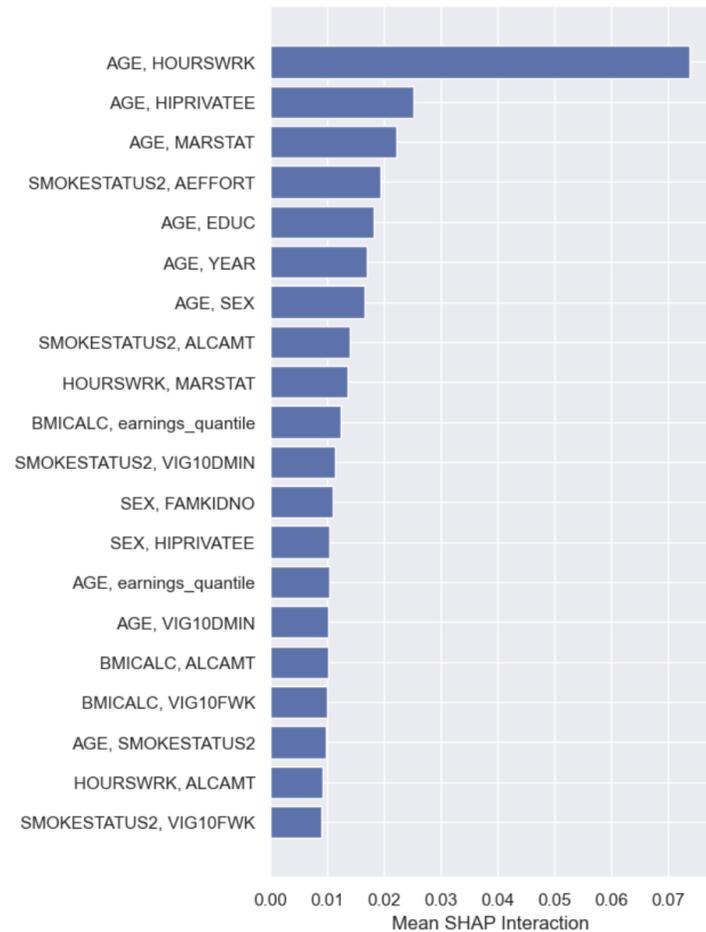
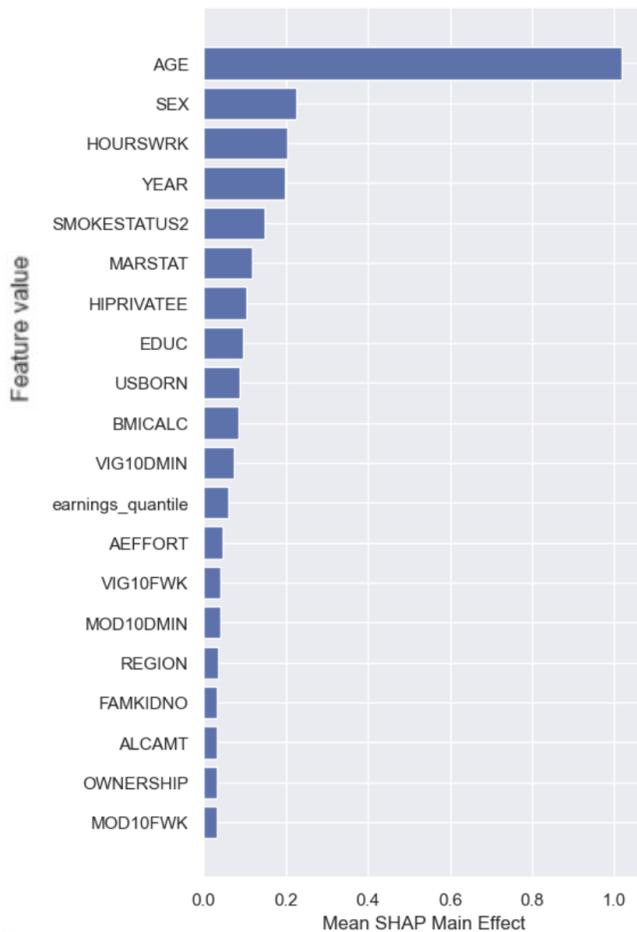
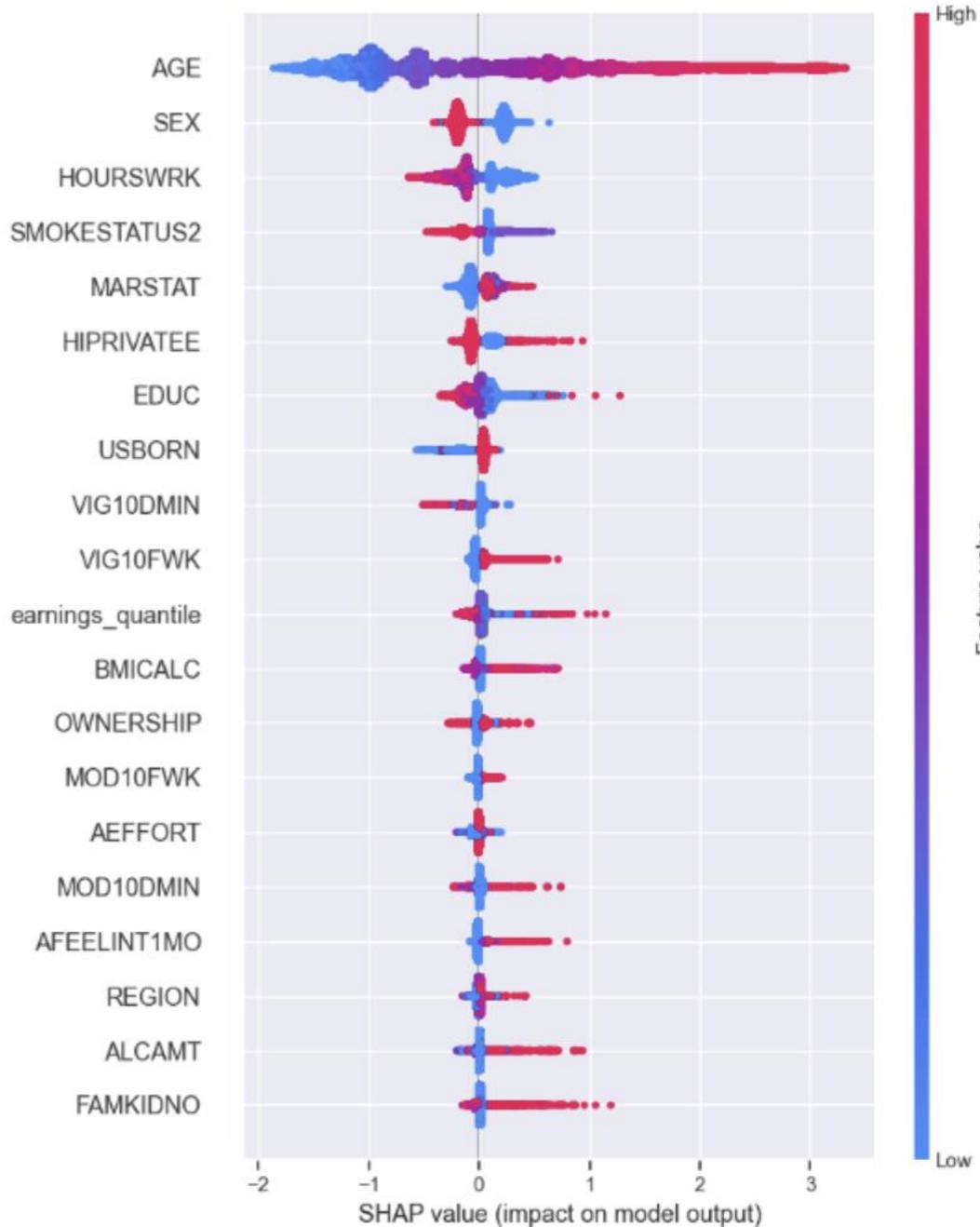


lifelines forest plot





# The dataset



## Other survival models

Model	Parameterization	Comments
Cox proportional hazards	$h(t \mathbf{x}) = h_0(t) \exp(\beta_1 x_1 + \dots)$	Proportional hazards, de facto standard

## Other survival models

Model	Parameterization	Comments
Cox proportional hazards	$h(t \mathbf{x}) = h_0(t) \exp(\beta_1 x_1 + \dots)$	Proportional hazards, de facto standard
Accelerated Failure Time (AFT)	$T = \exp(\varepsilon) \exp(\beta_1 x_1 + \dots)$	Scaling survival time

## Other survival models

Model	Parameterization	Comments
Cox proportional hazards	$h(t \mathbf{x}) = h_0(t) \exp(\beta_1 x_1 + \dots)$	Proportional hazards, de facto standard
Accelerated Failure Time (AFT)	$T = \exp(\varepsilon) \exp(\beta_1 x_1 + \dots)$	Scaling survival time
Survival trees	$S(t \mathbf{x}) = S_l(t)$ , where $l$ is $\mathbf{x}$ 's leaf	Log-rank test to split tree, Kaplan-Meier

## Other survival models

Model	Parameterization	Comments
Cox proportional hazards	$h(t \mathbf{x}) = h_0(t) \exp(\beta_1 x_1 + \dots)$	Proportional hazards, de facto standard
Accelerated Failure Time (AFT)	$T = \exp(\varepsilon) \exp(\beta_1 x_1 + \dots)$	Scaling survival time
Survival trees	$S(t \mathbf{x}) = S_l(t)$ , where $l$ is $\mathbf{x}$ 's leaf	Log-rank test to split tree, Kaplan-Meier
Random survival forest	$S(t \mathbf{x}) = \frac{1}{B} \sum_b S_l^{(b)}(t)$	Tree ensemble of survival trees

## Other survival models

Model	Parameterization	Comments
Cox proportional hazards	$h(t \mathbf{x}) = h_0(t) \exp(\beta_1 x_1 + \dots)$	Proportional hazards, de facto standard
Accelerated Failure Time (AFT)	$T = \exp(\varepsilon) \exp(\beta_1 x_1 + \dots)$	Scaling survival time
Survival trees	$S(t \mathbf{x}) = S_l(t)$ , where $l$ is $\mathbf{x}$ 's leaf	Log-rank test to split tree, Kaplan-Meier
Random survival forest	$S(t \mathbf{x}) = \frac{1}{B} \sum_b S_l^{(b)}(t)$	Tree ensemble of survival trees
Gradient boosted survival	$h(t \mathbf{x}) = h_0(t) \exp(f^{(m)}(\mathbf{x}))$	Iterative tree refinement $f^{(0)}, f^{(1)}, \dots, f^{(m)}$

## Other survival models

Model	Parameterization	Comments
Cox proportional hazards	$h(t \mathbf{x}) = h_0(t) \exp(\beta_1 x_1 + \dots)$	Proportional hazards, de facto standard
Accelerated Failure Time (AFT)	$T = \exp(\varepsilon) \exp(\beta_1 x_1 + \dots)$	Scaling survival time
Survival trees	$S(t \mathbf{x}) = S_l(t)$ , where $l$ is $\mathbf{x}$ 's leaf	Log-rank test to split tree, Kaplan-Meier
Random survival forest	$S(t \mathbf{x}) = \frac{1}{B} \sum_b S_l^{(b)}(t)$	Tree ensemble of survival trees
Gradient boosted survival	$h(t \mathbf{x}) = h_0(t) \exp(f^{(m)}(\mathbf{x}))$	Iterative tree refinement $f^{(0)}, f^{(1)}, \dots, f^{(m)}$
DeepSurv	$h(t \mathbf{x}) = h_0(t) \exp(z_\theta(\mathbf{x}))$	Neural network $z_\theta(\mathbf{x})$ , likelihood, early stopping

## Other survival models

Model	Parameterization	Comments
Cox proportional hazards	$h(t \mathbf{x}) = h_0(t) \exp(\beta_1 x_1 + \dots)$	Proportional hazards, de facto standard
Accelerated Failure Time (AFT)	$T = \exp(\varepsilon) \exp(\beta_1 x_1 + \dots)$	Scaling survival time
Survival trees	$S(t \mathbf{x}) = S_l(t)$ , where $l$ is $\mathbf{x}$ 's leaf	Log-rank test to split tree, Kaplan-Meier
Random survival forest	$S(t \mathbf{x}) = \frac{1}{B} \sum_b S_l^{(b)}(t)$	Tree ensemble of survival trees
Gradient boosted survival	$h(t \mathbf{x}) = h_0(t) \exp(f^{(m)}(\mathbf{x}))$	Iterative tree refinement $f^{(0)}, f^{(1)}, \dots, f^{(m)}$
DeepSurv	$h(t \mathbf{x}) = h_0(t) \exp(z_\theta(\mathbf{x}))$	Neural network $z_\theta(\mathbf{x})$ , likelihood, early stopping
DeepHit	Discrete version of PDF $f(t \mathbf{x})$	Neural network with softmax as last layer, allows to model <b>competing risks</b>

## Other survival models

Model	Parameterization	Comments
Cox proportional hazards	$h(t \mathbf{x}) = h_0(t) \exp(\beta_1 x_1 + \dots)$	Proportional hazards, de facto standard
Accelerated Failure Time (AFT)	$T = \exp(\varepsilon) \exp(\beta_1 x_1 + \dots)$	Scaling survival time
Survival trees	$S(t \mathbf{x}) = S_l(t)$ , where $l$ is $\mathbf{x}$ 's leaf	Log-rank test to split tree, Kaplan-Meier
Random survival forest	$S(t \mathbf{x}) = \frac{1}{B} \sum_b S_l^{(b)}(t)$	Tree ensemble of survival trees
Gradient boosted survival	$h(t \mathbf{x}) = h_0(t) \exp(f^{(m)}(\mathbf{x}))$	Iterative tree refinement $f^{(0)}, f^{(1)}, \dots, f^{(m)}$
DeepSurv	$h(t \mathbf{x}) = h_0(t) \exp(z_\theta(\mathbf{x}))$	Neural network $z_\theta(\mathbf{x})$ , likelihood, early stopping
DeepHit	Discrete version of PDF $f(t \mathbf{x})$	Neural network with softmax as last layer, allows to model <b>competing risks</b>
Deep Survival Machines	Mixture of Weibull or log-normal	Distribution parameters via neural networks

## Other survival models

Model	Parameterization	Comments
Cox proportional hazards	$h(t \mathbf{x}) = h_0(t) \exp(\beta_1 x_1 + \dots)$	Proportional hazards, de facto standard
Accelerated Failure Time (AFT)	$T = \exp(\varepsilon) \exp(\beta_1 x_1 + \dots)$	Scaling survival time
Survival trees	$S(t \mathbf{x}) = S_l(t)$ , where $l$ is $\mathbf{x}$ 's leaf	Log-rank test to split tree, Kaplan-Meier
Random survival forest	$S(t \mathbf{x}) = \frac{1}{B} \sum_b S_l^{(b)}(t)$	Tree ensemble of survival trees
Gradient boosted survival	$h(t \mathbf{x}) = h_0(t) \exp(f^{(m)}(\mathbf{x}))$	Iterative tree refinement $f^{(0)}, f^{(1)}, \dots, f^{(m)}$
DeepSurv	$h(t \mathbf{x}) = h_0(t) \exp(z_\theta(\mathbf{x}))$	Neural network $z_\theta(\mathbf{x})$ , likelihood, early stopping
DeepHit	Discrete version of PDF $f(t \mathbf{x})$	Neural network with softmax as last layer, allows to model <b>competing risks</b>
Deep Survival Machines	Mixture of Weibull or log-normal	Distribution parameters via neural networks
Transformer based survival	Discrete version of PDF $f(t \mathbf{x})$	Transformer based neural network that can consider full <b>longitudinal data</b>

## Survival model performance metrics

- **C-index:** let  $P$  be the set of *comparable* individuals  $(i, j)$ , i.e.,  $\delta_i = 1$  and  $t_i < t_j$ ,

$$\text{C-index} = \frac{1}{\#P} \sum_{(i,j) \in P} \mathbb{I}_{h(t_i|\mathbf{x}_i) > h(t_j|\mathbf{x}_j)}$$

- **Integrated Brier score (IBS):**

$$\text{IBS} = \int_0^\tau \frac{1}{n} \sum_{i=1}^n w_i(t) (\mathbb{I}_{t_i > t} - S(t|\mathbf{x}_i))^2, \text{ where } w_i(t) \text{ are inverse probability censoring weights}$$

- **Log-loss in time interval (LL):** let  $y_i(t_1, t_2)$  be the indicator whether individual  $i$  had an event in  $[t_1, t_2)$ ,

$$\text{LL} = -\frac{1}{n} \sum_{i=1}^n y_i(t_1, t_2) \log(S(t_1|\mathbf{x}_i) - S(t_2|\mathbf{x}_i)) + (1 - y_i(t_1, t_2)) \log(1 - S(t_1|\mathbf{x}_i) + S(t_2|\mathbf{x}_i))$$

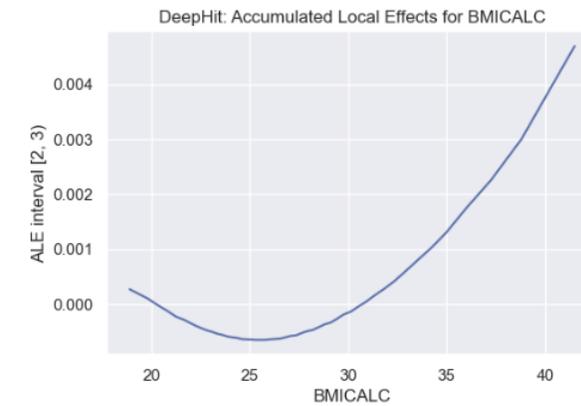
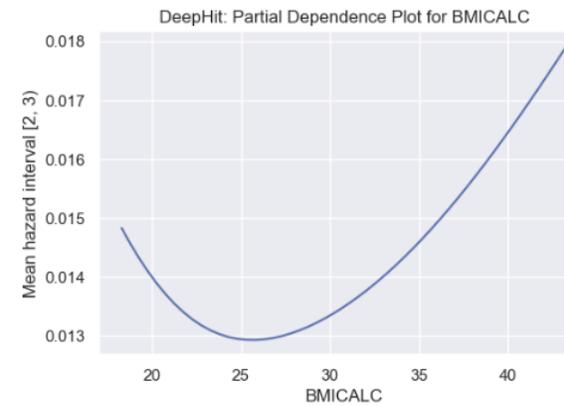
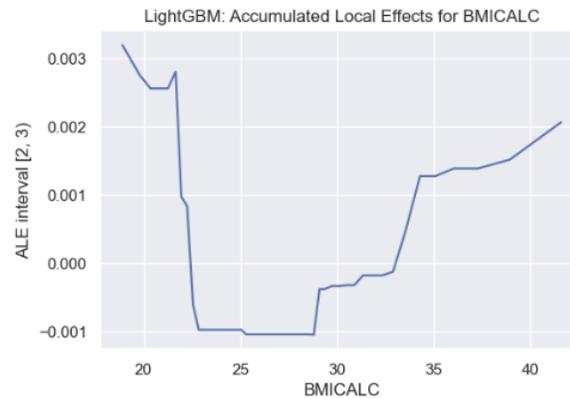
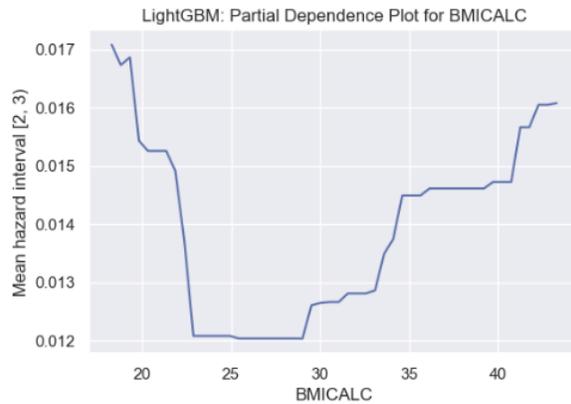
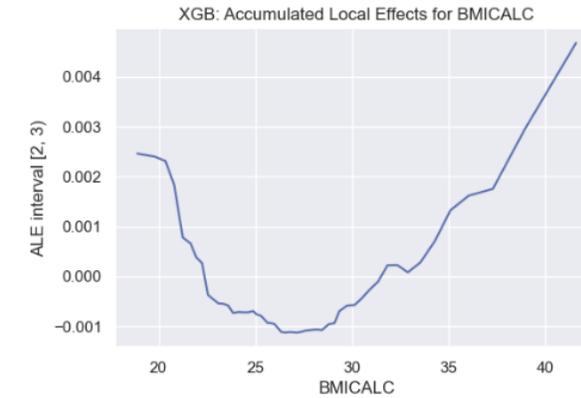
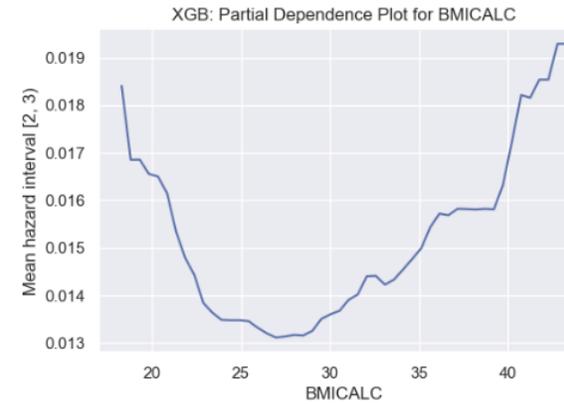
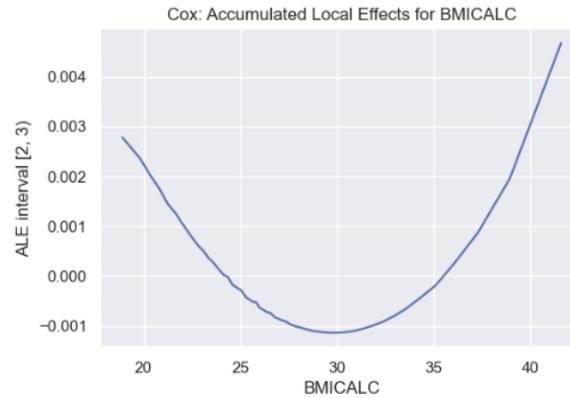
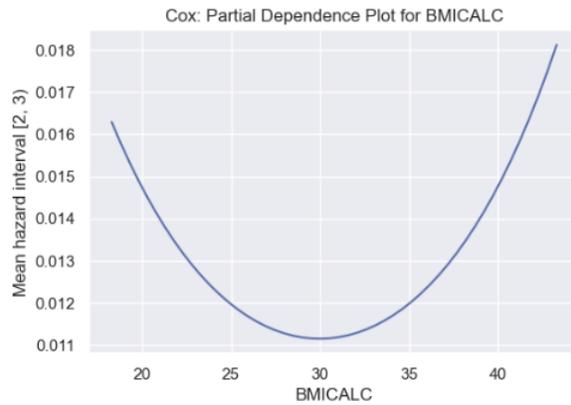
- **Mean squared error (MSE) of log predictions:** let  $\mu_i(t_1, t_2)$  denote the ground truth probability

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (\log(S(t_1|\mathbf{x}_i) - S(t_2|\mathbf{x}_i)) - \log \mu_i(t_1, t_2))^2$$

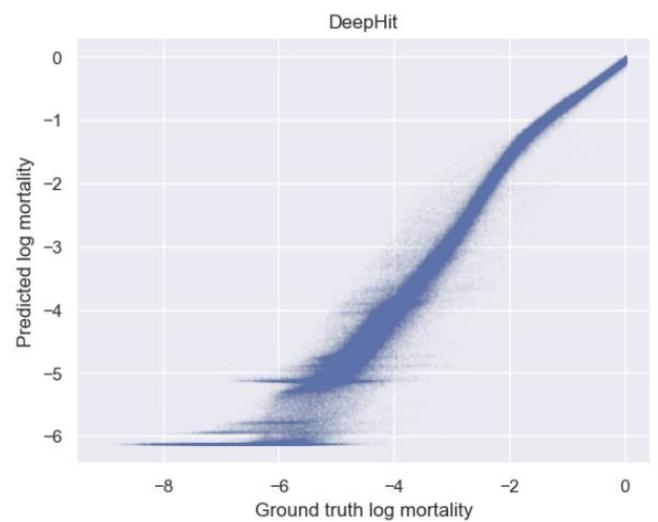
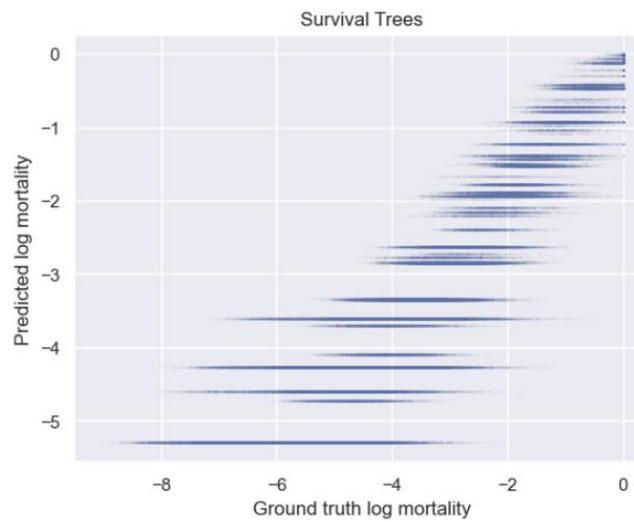
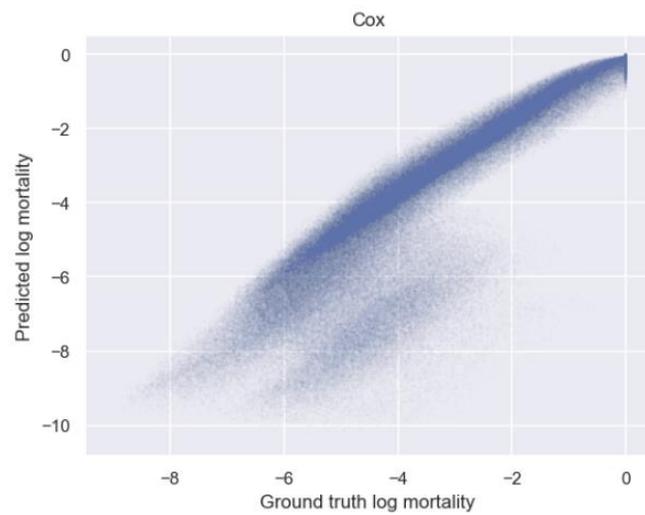
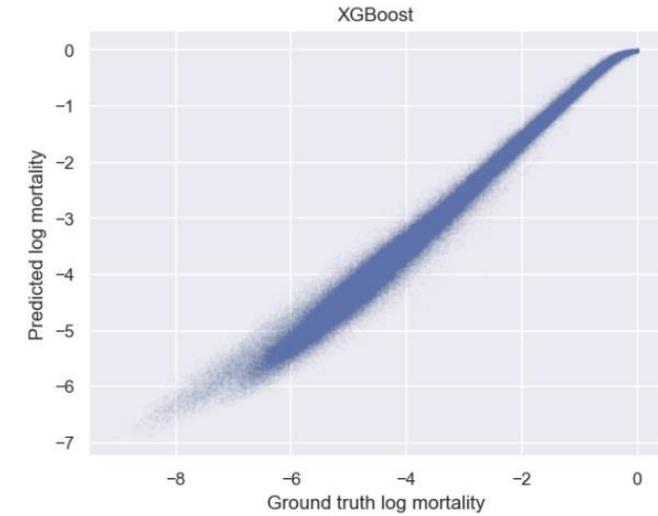
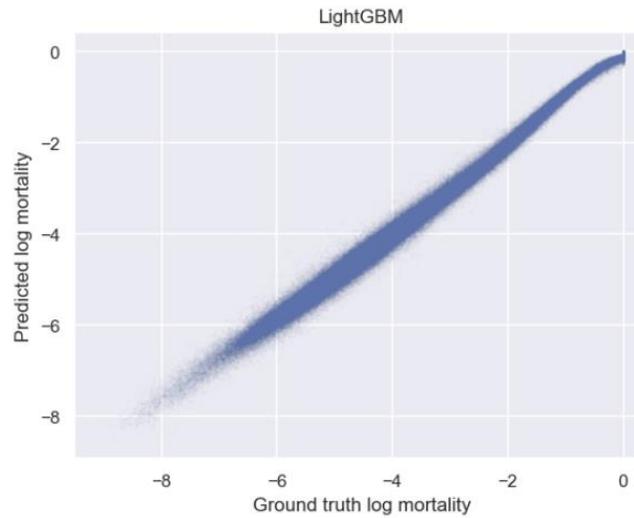
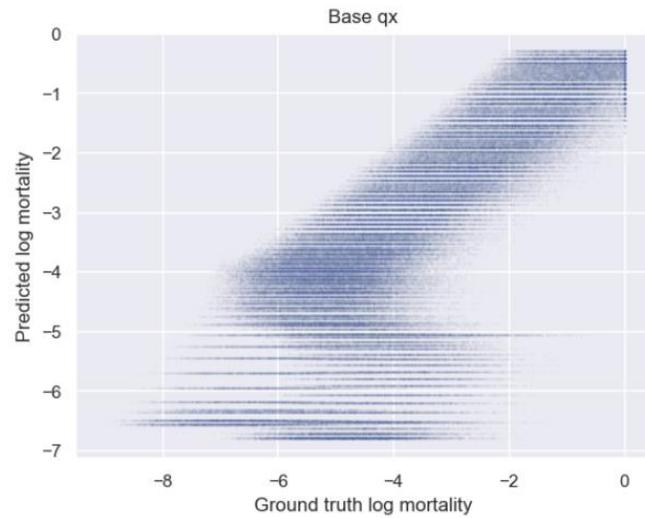
## Survival model performance metrics

	C-index ↑	IBS ↓	LL [2, 3) ↓	Time [min] ↓
Base $q_x$	0.8402	0.0439	0.0519	<1
LightGBM	0.8599	0.0415	<b>0.0502</b>	<1
Cox Proportional Hazards	0.8612	0.0417	0.0504	<1
Accelerated Failure Time	0.8612	0.0425	0.0517	<1
Survival Trees	0.8570	0.0415	0.0512	4
Random Survival Forests	0.8682	0.0412	0.0507	491
Gradient Boosted Survival Trees	0.8701	0.0412	0.0507	444
XGBoost Cox	0.8724	0.0410	0.0512	<1
DeepSurv	0.8711	<b>0.0393</b>	0.0511	<1
DeepHit	<b>0.8781</b>	0.0407	0.0515	4
Deep Survival Machines	0.8705	0.0423	0.0509	5
Transformer Survival Model	0.8689	0.0396	0.0504	337

# Partial dependence plots and accumulated local effects



# Ground truth vs. predictions on a larger synthetic dataset



## Tips and tricks and pitfalls

1. Start with a fast and strong model, e.g., LightGBM (interval event prediction) or XGBoost (survival)
2. For (Life & UW) actuarial purposes, MSE on log predictions is probably the best performance metric – if the ground truth is known
3. If the ground truth is not known, try to predict it with the models from 1., potentially simulating a new dataset – as a learning experience to choose a deep learning model if you have sufficient data
4. Don't underestimate the many pitfalls of survival modelling:
  - off-by-one errors or other discretization issues on the time dimension
  - selection effects for early times
  - missing values (not at random)
  - time-dependencies, e.g., current vs. past BMI
  - miscalibrated models, e.g., overestimating risk of low risk individuals
  - slow running times

Any  
questions?

# Thank you!

## Contact us



Daniel Meier

L&H R&D Manager  
daniel\_meier@swissre.com

## Follow us



# Legal notice

©2025 Swiss Re. All rights reserved. You may use this presentation for private or internal purposes but note that any copyright or other proprietary notices must not be removed. You are not permitted to create any modifications or derivative works of this presentation, or to use it for commercial or other public purposes, without the prior written permission of Swiss Re.

The information and opinions contained in the presentation are provided as at the date of the presentation and may change. Although the information used was taken from reliable sources, Swiss Re does not accept any responsibility for its accuracy or comprehensiveness or its updating. All liability for the accuracy and completeness of the information or for any damage or loss resulting from its use is expressly excluded.